

The Hot Horizontal-Branch Stars in NGC 288 – Effects of Diffusion and Stratification on Their Atmospheric Parameters[★]

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ABSTRACT

Context. NGC 288 is a globular cluster with a well developed blue horizontal branch covering the so-called u -jump which indicates the onset of diffusion. It is therefore well suited to study the effects of diffusion in blue horizontal branch (HB) stars.

Aims. We compare observed abundances to predictions from stellar evolution models calculated with diffusion and from stratified atmospheric models. We verify the effect of using stratified model spectra to derive atmospheric parameters. In addition we investigate the nature of the overluminous blue HB stars around the u -jump.

Methods. We define a new photometric index sz from $uvby$ measurements that is gravity sensitive between 8 000 K and 12 000 K. Using medium-resolution spectra and Strömgren photometry we determine atmospheric parameters (T_{eff} , $\log g$) and abundances for the blue HB stars. We use both homogeneous and stratified model spectra for our spectroscopic analyses.

Results. The atmospheric parameters and masses of the hot HB stars in NGC 288 show a behaviour seen also in other clusters for temperatures between 9 000 K and 14 000 K. Outside this temperature range, however, they follow rather the results found for such stars in ω Cen. The abundances derived from our observations are for most elements (except He and P) within the abundance range expected from evolutionary models that include the effects of atomic diffusion and assume a surface mixed mass of $10^{-7} M_{\odot}$. The abundances predicted by stratified model atmospheres are generally significantly more extreme than observed, except for Mg. The use of stratified model spectra to determine effective temperatures, surface gravities and masses moves the hotter stars to a closer agreement with canonical evolutionary predictions.

Conclusions. Our results show definite promise towards solving the long-standing issue of surface gravity and mass discrepancies for hot HB stars, but there is still much work needed to arrive at a self-consistent solution.

Key words. Stars: horizontal branch – Stars: atmospheres – Techniques: spectroscopic – globular clusters: individual: NGC 288

1. Introduction

Low-mass stars burning helium in a core of about $0.5 M_{\odot}$ and hydrogen in a shell populate a roughly horizontal region in the optical colour-magnitude diagrams of globular clusters, which has earned them the name “horizontal-branch” (**HB**) stars (ten Bruggencate, 1927). The hot (or blue) HB stars near an effective temperature of 11 500 K are of special interest because they

exhibit a number of intriguing phenomena associated with the onset of diffusion.

1.1. Diffusion

A large photometric survey of many globular clusters by Grundahl et al. (1999) demonstrated that the Strömgren u -brightness of blue HB stars suddenly increases near 11 500 K. This so-called u -jump is attributed to a sudden increase in the atmospheric metallicity of the blue HB stars to super-solar val-

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ues, due to the *radiative levitation of heavy elements*. A similar effect can be seen in broad-band $U, U - V$ photometric data (Ferraro et al. 1998, G1). The work of Behr et al. (1999, 2000b) and Moehler et al. (2000) confirmed with direct spectroscopic evidence that the atmospheric metallicity does indeed increase to solar or super-solar values for HB stars hotter than the u -jump. A list of earlier observations of this effect can be found in Moehler (2001, Sect. 2.4). Later studies include Behr (2003, M 3, M 13, M 15, M 68, M 92, and NGC 288), Fabbian et al. (2005, NGC 1904), and Pace et al. (2006, NGC 2808). These findings also helped to understand the cause of the so-called “low-gravity” problem: Crocker et al. (1988) and Moehler et al. (1995, 1997) found that hot horizontal branch stars – when analysed with model spectra of the same metallicity as their parent globular cluster – show significantly lower surface gravities than expected from evolutionary tracks. Analysing them instead with more appropriate metal-rich model spectra reduces the discrepancies considerably (Moehler et al. 2000). The more realistic stratified model atmospheres of Hui-Bon-Hoa et al. (2000) and LeBlanc et al. (2009) reduce the discrepancies in surface gravity even further (see below for more details). Along with the enhancement of heavy metals a decrease in the helium abundance by mass Y is observed for stars hotter than $\approx 11\,500$ K, while cooler stars have normal helium abundances within the observational errors. The helium abundance for these hotter stars is typically between 1 and 2 dex smaller than the solar value (e.g. Behr 2003). A trend of the helium abundance relative to T_{eff} was discussed by Moni Bidin et al. (2009, 2012). Finally, blue HB stars near $\approx 11\,500$ K show a sudden drop in their rotation rates (Peterson et al. 1995, Behr et al. 2000a and Behr 2003), and in some globular clusters (e.g., M 13) a gap in their HB distribution.

The possibility of *radiative levitation of heavy elements* and *gravitational settling of helium* in HB stars had been predicted long ago by Michaud et al. (1983), but the discovery of its very sudden onset near 11 500 K was a complete surprise. Quievy et al. (2009) have shown that helium settling in HB stars cooler than $\approx 11\,500$ K is hampered by meridional flow. In stars hotter than this threshold, helium may settle and the superficial convection zone disappears and therefore diffusion may come at play in superficial regions of these stars. Recent evolutionary models of HB stars that include atomic diffusion calculated by Michaud et al. (2008, 2011) can reproduce the abundance anomalies of several elements observed in blue HB stars reasonably well. However, these models do not treat the atmospheric region in detail. Instead they assume an outer superficial mixed zone of approximately $10^{-7} M_{\odot}$ below which separation occurs.

The detection of vertical stratification of some elements, especially iron, in the atmospheres of blue HB stars lends additional support to the presence of atomic diffusion there (Khalack et al. 2007, 2008, 2010), but is at variance with the mixed zone introduced by Michaud et al. (2008, 2011). Hui-Bon-Hoa et al. (2000) and LeBlanc et al. (2009) present stellar atmosphere models of blue HB stars which include the effect of vertical abundance stratification on the atmospheric structure. These models estimate the vertical stratification of the elements caused by diffusion by assuming that an equilibrium solution

(i.e. giving a nil diffusion velocity) for each species is reached. Assuming a sudden onset of atomic diffusion near 11 500 K, these models predict photometric jumps and gaps (Grundahl et al. 1999, G1 in Ferraro et al. 1998) consistent with observations (see LeBlanc et al. 2010 for more details). The photometric changes, as compared to chemically homogeneous atmosphere models, are due to the modification of the atmospheric structure caused by the abundance stratification.

1.2. NGC 288

The u -jump described above can be clearly seen in the colour-magnitude diagram of NGC 288 shown in Fig. 1, where one also finds a group of stars with large (and unexplained) scatter in their u magnitudes and $(u-y)$ colours around the jump region (triangles in Fig. 1). With maximum errors of $0.^m008$ in u and $0.^m003$ in y it is unlikely that their positions are caused by photometric errors. The evolutionary status of these stars is unclear. While their bright u magnitudes are suggestive of radiative levitation, the effect would have to be extreme and some of them appear to lie on the cool side of the u -jump. Similar groups of unexpectedly bright stars can be found in other globular clusters (see M 2 and M 92 in Grundahl et al. 1999), with NGC 288 presenting the most pronounced case. We refer the reader to Sect. 8 for a more detailed discussion.

A colour spread along the red giant branch in NGC 288 first reported by Yong et al. (2008) was identified as a split by Roh et al. (2011), which was confirmed by Carretta et al. (2011) and Monelli et al. (2013). In their excellent review on second and third parameters to explain the horizontal-branch morphology, Gratton et al. (2010) estimated that a range in helium abundance of $\Delta Y = 0.012$ would explain the temperature range of the horizontal branch in NGC 288. This is consistent with the helium range found more recently from the analysis of main sequence photometry by Piotto et al. (2013). Such a small variation in helium is unfortunately too small to be detected by our analysis.

2. Observations

The targets were selected from the Strömgren photometry of Grundahl et al. (1999). We selected 71 blue horizontal-branch star candidates (see Fig. 1) and 17 red giants. Of the blue HB candidates three turned out to be red HB stars and one had extremely noisy spectra. In this paper we discuss only the observations of the 67 bona-fide hot horizontal-branch stars (see Table 1 for their coordinates and photometric measurements).

The spectroscopic data were obtained between July 3 and 27, 2003 (date at the beginning of the night, see Table 2 for details) in Service Mode using the multi-object fibre spectrograph FLAMES+GIRAFFE (Pasquini et al. 2000), which is mounted at the UT2 Telescope of the VLT. The fibre systems MEDUSA1 and MEDUSA2 allow to observe up to 132 objects simultaneously. We used the low spectroscopic resolution mode with the spectral ranges $3620 - 4081$ Å (LR1, $\lambda/\Delta\lambda = 8000$), $3964 - 4567$ Å (LR2, $\lambda/\Delta\lambda = 6400$) and $4501 - 5078$ Å (LR3, $\lambda/\Delta\lambda = 7500$). GIRAFFE had a $2k \times 4k$ EEV CCD chip ($15\mu\text{m}$ pixel size), with a gain of $0.54 \text{ e}^- \text{ ADU}^{-1}$ and a read-out

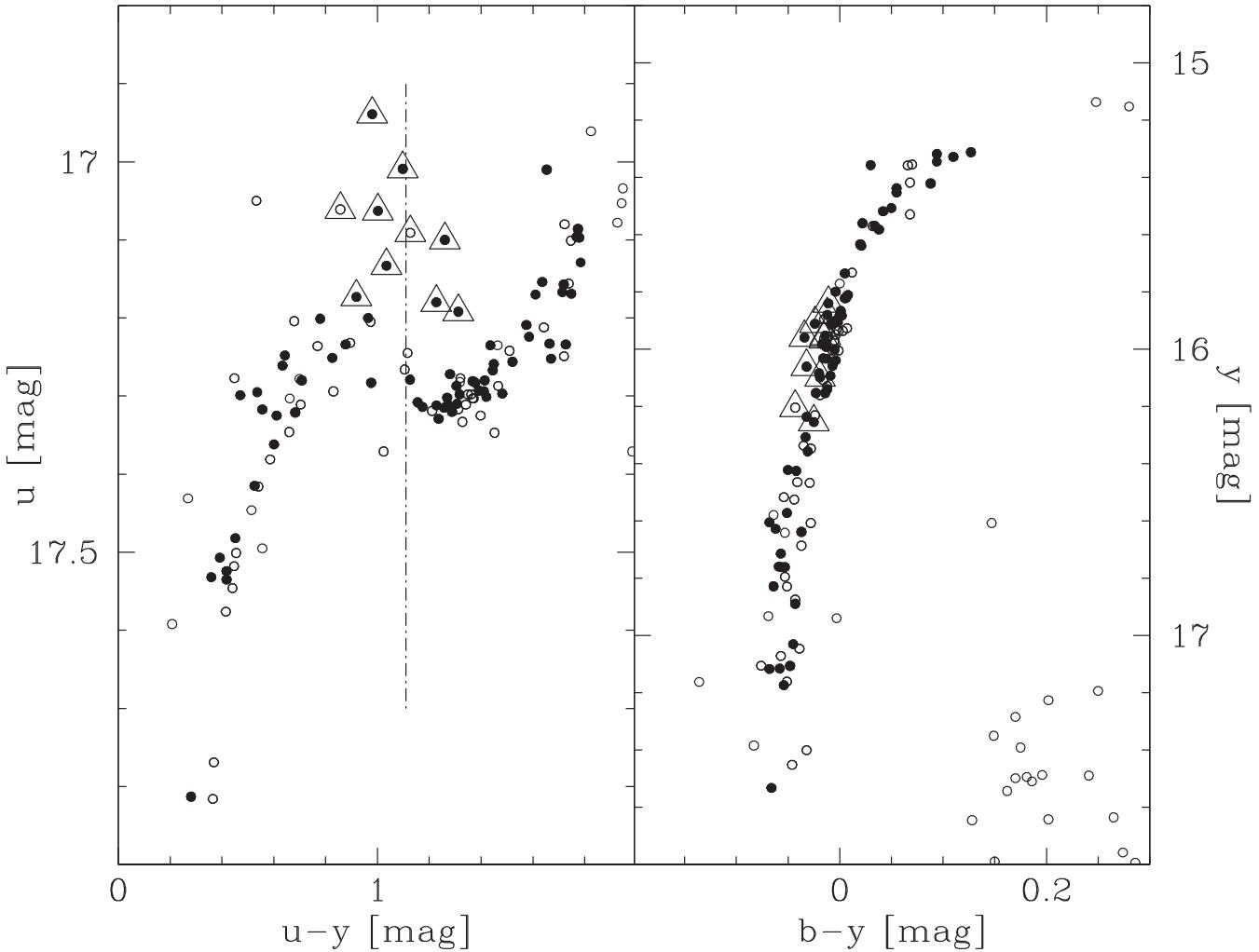


Fig. 1. The blue HB stars in NGC 288 as observed by Grundahl et al. (1999). The subsample, for which GIRAFFE spectra were observed, is marked by filled circles. The dot-dashed line in the left part marks the $u - y$ colour of the u -jump. Stars on the red side of the line do not show evidence for radiative levitation, while stars on the blue side do. The triangles mark overluminous stars around the u -jump (from red to blue: 122, 103, 127, 101, 146, 142, 100, 183).

noise of 3.2 e^- . Each night four screen flat fields, five bias, and one ThAr wavelength calibration frame were observed. In addition to the daytime ThAr spectra covering all fibres, we also observed simultaneous ThAr spectra during the science observations in five of the fibres. Dark exposures were not necessary, because the dark current of $2 \text{ e}^- \text{ h}^{-1} \text{ pixel}^{-1}$ is negligible.

3. Data reduction

The spectroscopic data were reduced using the girBLDRS software (<http://girblrs.sourceforge.net/>, version 1.10) and ESO MIDAS (see Drews 2005 for details). The 2-dimensional bias and flat field frames were averaged for each night. The averaged flat fields were used to determine the positions and widths of the fibre spectra. 64-pixel portions of each fibre spectrum were averaged and fitted with a point spread function (PSF). A polynomial fit to the PSF parameters then provides the PSF for the whole frame, which is used for all extractions later on. The one-dimensional flat field spectra extracted using Horne's

method (Horne 1986) are the so-called “narrow flat-fields” (nff), which are used to correct the extracted science spectra for spectrograph and detector signature. As the nff spectra are not normalised they still show the spectral signature of the flat field lamp, which however varies slowly with wavelength.

The daytime Th-Ar wavelength calibration spectra were extracted for each fibre via a simple sum, the spectral lines localised and fit by an analytical model. The presence of simultaneous ThAr spectra in the science frames allowed us to refine the localisation and wavelength calibration of the science data by correcting for residual wavelength shifts between daytime and nighttime observations. The refinement was repeated until the difference between the observed ThAr positions and the laboratory ones was below 0.001 km s^{-1} . The wavelength offsets obtained from the cross-correlation are then linearly interpolated across the CCD (spatial direction), and the interpolated offsets are applied to each fibre.

The raw science spectra were bias and flatfield corrected and finally rebinned to constant wavelength steps. The median

of the sky signal obtained in 18 dedicated fibres was subtracted from the science data.

The spectra for a given star and setup were then normalised as described in Moehler et al. (2011) taking care to use only regions free from strong lines for the continuum definition. This normalisation allows us to exclude outlying pixels during the averaging of the spectra.

4. Radial velocities

After the barycentric correction, the observed spectra were first co-added (without further radial velocity correction) and fitted with stellar model spectra to get a first estimate of their effective temperatures, surface gravities, and helium abundances (see Sect. 5.2 for details). The individual spectra of each star were then cross-correlated (see Tonry & Davis 1979 for more details) with the best fitting synthetic spectrum derived this way. Only regions of hydrogen or helium lines were selected prior to the cross-correlation. The peak of the cross-correlation function was fitted with a Gaussian function to determine the radial velocity to sub-resolution accuracy. The velocity-corrected spectra were co-added and fitted with synthetic model atmospheres (see Sect. 5). In a second step, the best-fit synthetic spectra were then used to repeat the cross-correlation. The 1σ errors in radial velocity for individual spectra range from 1.8 km s^{-1} to up to 10 km s^{-1} depending on the quality. The median error is 2.7 km s^{-1} .

For each star, we calculated the standard deviation of the radial velocity measurements of the individual spectra. We then counted, how many of the individual measurements deviate more than 1σ from the mean. In none of the stars this was larger than 30%, i.e. the scatter is consistent with a random distribution within the measurement error. We thus find no evidence for radial velocity variations that might indicate the presence of close binaries in our sample. **We note that this absence of evidence should not be confused with an evidence of absence, i.e. we cannot say anything about the frequency of binaries among our target stars, as neither our method nor our observations were tailored towards the detection of binaries.** There is also no evidence for field contamination in our sample.

The radial velocities of the 67 stars range from -48.6 km s^{-1} to -36.9 km s^{-1} with a median value of $-42.6 \pm 2.7 \text{ km s}^{-1}$, that is close to the average value of -45.4 km s^{-1} given by Harris (1996) and to the recently published values of -43.5 km s^{-1} (Székely et al. 2007, uncertainty $1-2 \text{ km s}^{-1}$), $-46.15 \pm 2.55 \text{ km s}^{-1}$ (Carretta et al. 2009a), and $-45.1 \pm 0.2 \text{ km s}^{-1}$ (Lane et al. 2010).

Each spectrum was corrected to laboratory wavelength. As an additional safeguard against outliers only a subset of pixel values around the median (11 out of 13 for LR1, 5 out of 7 for LR2, 3 out of 5 for LR3) was averaged. In order to allow a combination of the three wavelength ranges into one spectrum for fitting the LR1 data were convolved with a Gaussian with a FWHM of 0.48 \AA to have the same resolution for all three regions.

5. Atmospheric Parameters

5.1. Determination from photometric data

We used the Strömgren photometry of Grundahl et al. (1999) to get a first estimate of the effective temperatures and surface gravities of the stars redwards of the u -jump, similar to our work in Moehler et al. (2003). As reference we used theoretical colours from Kurucz (ATLAS9, 1993) for metallicities $[\text{M}/\text{H}] = -1.0$ and -1.5 . The metallicity $[\text{Fe}/\text{H}]$ of NGC 288 given by Carretta et al. (2009b) is -1.32 . Unfortunately we have no H_β photometry for the stars. Therefore, guided by the equations of Moon & Dworetsky (1985) we looked for a combination of colours that provides a rectangular grid in the T_{eff} , $\log g$ plane for the range $8000 \text{ K} \leq T_{\text{eff}} \leq 12000 \text{ K}$. We used the definition for a_0 from Moon & Dworetsky, but we defined in addition an index sz as follows

$$a_0 = 1.36 \cdot (b - y) + 0.36 \cdot m_1 + 0.18 \cdot c_1 - 0.2448$$

$$sz = -0.07 \cdot (b - y) - m_1 + 0.1 \cdot c_1 + 0.1$$

As one can see from Fig. 2 a_0 correlates with T_{eff} and sz correlates with $\log g$ and T_{eff} . The photometric data were dereddened with $E_{\text{B-V}} = 0^{\text{m}}03$ (Carretta et al. 2000), using $E_{\text{b-y}} = 0.75 \cdot E_{\text{B-V}}$.

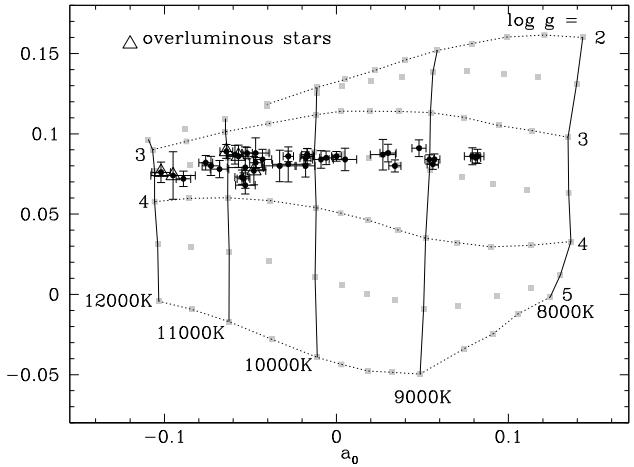


Fig. 2. Theoretical a_0, sz grid as derived from Kurucz (1993) colours for $[\text{Fe}/\text{H}] = -1.5$. In addition we show the positions of the cool blue HB stars (i.e. redward of the vertical line in Fig. 1) in this diagram as observed by Grundahl et al. (1999).

To restrict the range of fitting we used only $\log g$ between 3 and 4 and T_{eff} between 8000 K and 12000 K . We fitted a 2nd order polynomial to the relation $T_{\text{eff}}(a_0)$, which yielded an rms deviation of 30 K. For the surface gravities we fitted 2nd order polynomials to the relation $\log g(a_0, sz)$, which yielded an rms deviation of 0.04 in $\log g$. Temperatures and surface gravities derived from these relations are listed in Table 3 and plotted in Fig. 3 for stars cooler than the u -jump.

The errors provided in Table 3 are a quadratic combination of errors from the photometric data, the uncertainty of the reddening in the y band (estimated to be $0^{\text{m}}02$) and the error of the

fit to the theoretical relations. In order to have an estimate of the influence of metallicity we compared the results obtained for the two metallicities mentioned above. The differences in temperature vary almost linearly from -0.1% at 8000 K to $+0.8\%$ at 12000 K , with the results from the more metal-poor models being hotter at the hot end. The differences are therefore well below the errors on the individual temperatures.

The differences in surface gravities for these two metallicities show a quadratic dependency on the effective temperature, varying from $+0.02$ at about 8600 K (with the surface gravities from the metal-poor models being higher at 8600 K than those from the more metal-rich models) to 0 at 9000 K and 11000 K via -0.02 at about 10000 K . For temperatures below 8500 K the differences increase to -0.08 , but those stars are too cool to be analysed spectroscopically with our methods (see Sect. 5.2). Within the temperature range of interest for further analysis the differences are below the average errors of the surface gravities given in Table 3. For reasons of consistency between photometric and spectroscopic analysis we decided against averaging the photometric grids.

Taking together the errors listed in Table 3 and the uncertainties due to the metallicity, we estimate typical errors in T_{eff} and $\log g$ to be about 5% and 0.13 dex , respectively.

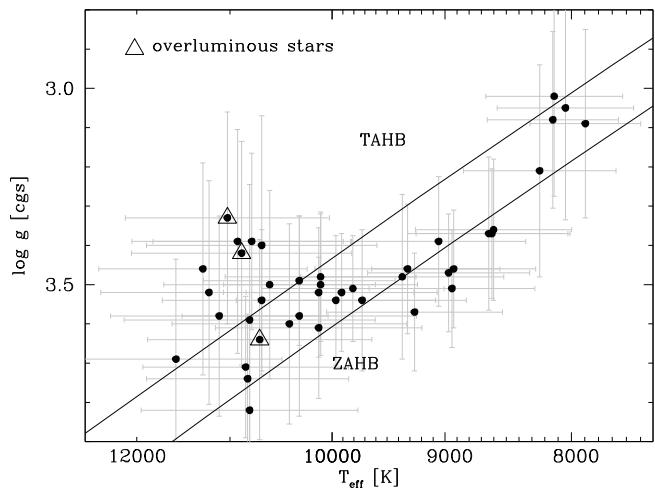


Fig. 3. Atmospheric parameters derived from the a_0, sz indices for stars not showing evidence for radiative levitation. For comparison we also show curves representing a canonical zero-age horizontal branch and terminal age horizontal branch from Moehler et al. (2003).

5.2. Line profile fitting with homogeneous model spectra

For the stars redder than the u -jump, we computed model atmospheres with convection for $[\text{M}/\text{H}] = -1.5$ using ATLAS9 (Kurucz 1993) and used Lemke's version¹ of the LINFOR program (developed originally by Holweger, Steffen, and

Steenbock at Kiel University) to compute a grid of theoretical spectra which include the Balmer lines H_α to H_{22} , He I and He II lines. The grid covers the range $7500\text{ K} \leq T_{\text{eff}} \leq 12000\text{ K}$, $2.5 \leq \log g \leq 5.0$, and $-3.0 \leq \log \frac{n_{\text{He}}}{n_{\text{H}}} \leq -1.0$. For the stars bluer than the u -jump we used model atmospheres computed for $[\text{M}/\text{H}] = +0.5$ (see Moehler et al. 2000 for details). From an extrapolation of the LTE/NLTE threshold for subdwarf B stars (Napiwotzki 1997) we assume that LTE is a valid approximation here as well. To establish the best fit to the observed spectra, we used the fitsb2 routines developed by Napiwotzki et al. (2004), which employ a χ^2 test. The σ necessary for the calculation of χ^2 is estimated from the noise in the continuum regions of the spectra. The fit program normalises synthetic model spectra and observed spectra using the same points for the continuum definition.

While the errors were obtained via boot strapping and should therefore be rather realistic, they do not include possible systematic errors due to, e.g., flat field inaccuracies or imperfect sky subtraction. The true errors in T_{eff} are probably close to those from photometry, i.e. 5% , and the true errors in $\log g$ are probably about 0.1 .

Because the χ^2 fit of the line profile can lead to ambiguous results for effective temperatures close to the Balmer maximum, the results from Sect. 5.1 are taken as initial parameters for the spectral line profile fitting procedure.

In Table 3 we list the results obtained from fitting the Balmer lines H_β to H_{10} (excluding H_ϵ to avoid the Ca II H line) in the cool stars. For the cool stars we did not fit the helium lines, as they are very weak and tend to produce spurious results. We verified, however, that the helium lines predicted by the model spectra with solar helium abundance did reproduce the observations. The reddest stars showing many strong metal lines (55, 60, 61, 63, 72) were omitted from the line profile fits because our model spectra contain only H and He lines. For the stars hotter than 11500 K we fitted in addition the He I lines at $\lambda\lambda 4026\text{\AA}, 4388\text{\AA}, 4472\text{\AA}$, and 4922\AA .

Fig. 4 shows a gap at $8500\text{ K} \leq T_{\text{eff}} \leq 9000\text{ K}$ in the atmospheric parameters derived from line profile fitting, that was first noted and discussed by Moehler et al. (2003) for observations of HB stars in M 13. The stars populating this region in Fig. 3 close to the zero-age horizontal branch (ZAHB) are in Fig. 4 at about 8000 K , above the terminal-age horizontal branch (TAHB). Prompted by the referee we treated a homogeneous model spectrum calculated for $T_{\text{eff}} = 8800\text{ K}, \log g = 3.35$ and $[\text{M}/\text{H}] = -1.5$ as described in Sect. 6.3 to simulate an observed spectrum. Varying the starting values of the fit from 8000 K to 9500 K for T_{eff} and 3.2 to 3.6 for $\log g$ did not affect the fit results which stayed at $T_{\text{eff}} = 8841\text{ K}$ and $\log g = 3.35$. Varying the FWHM of the Gaussian, with which the model spectra are convolved before fitting, from 0.6 \AA to 0.75 \AA resulted in T_{eff} between 8818 K and 8862 K and $\log g$ between 3.34 and 3.36 . We noted, however, that the resolution of the observed data seems to vary slightly with wavelength — at the blue end the predicted line profiles are very slightly wider and deeper than the observed ones, while for H_β the observed line core is slightly more narrow and deep. To rule out possible small variations in resolution across the wavelength range as the cause for the gap, we convolved the observed spectra to

¹ For a description see <http://a400.sternwarte.uni-erlangen.de/~ai26/linfit/linfor.html>

Table 4. Temperatures, surface gravities, and helium abundances from line profile fits for stars bluer than the u -jump and showing evidence of radiative levitation). The errors are derived from the χ^2 fit (see Sect. 5.2 for details) and are statistical errors only. In addition we list the helium abundance as determined with LINFOR (see Sect. 6 for details).

ID	T_{eff}	$\log g$	$\log \left(\frac{n_{\text{He}}}{n_{\text{H}}}\right)_{\text{fitsb2}}$	$\log \left(\frac{n_{\text{He}}}{n_{\text{H}}}\right)_{\text{LINFOR}}$
100	11400 ± 100	3.65 ± 0.03	-2.23 ± 0.11	-2.14
101	11400 ± 100	3.78 ± 0.03	-1.95 ± 0.11	-1.93
142	11400 ± 100	3.72 ± 0.03	-2.98 ± 0.12	-2.76
146	11600 ± 100	3.81 ± 0.03	-2.06 ± 0.10	-2.02
179	11600 ± 100	3.77 ± 0.03	-2.37 ± 0.10	-2.14
183	12300 ± 100	3.93 ± 0.03	-2.27 ± 0.12	-2.36
187	11700 ± 100	3.84 ± 0.03	-2.74 ± 0.13	-2.87
195	12400 ± 100	3.86 ± 0.03	-2.55 ± 0.15	-2.51
196	12300 ± 100	3.91 ± 0.03	-2.67 ± 0.18	-2.49
199	12400 ± 100	3.94 ± 0.03	-2.79 ± 0.18	-2.84
212	12900 ± 100	3.93 ± 0.02	-2.66 ± 0.12	-2.57
213	13100 ± 100	3.97 ± 0.03	-2.61 ± 0.15	-2.68
216	12900 ± 100	3.94 ± 0.02	-2.66 ± 0.14	-2.71
221	13200 ± 100	3.97 ± 0.03	-2.67 ± 0.13	-2.60
228	13800 ± 100	4.00 ± 0.03	-2.43 ± 0.17	-2.43
230	13800 ± 100	4.06 ± 0.03	-2.28 ± 0.10	-2.34
231	13300 ± 100	4.00 ± 0.02	-2.72 ± 0.09	-2.55
240	13300 ± 100	3.99 ± 0.03	-2.71 ± 0.11	-2.61
242	14300 ± 100	4.03 ± 0.03	-2.37 ± 0.13	-2.28
243	14400 ± 100	4.09 ± 0.04	-2.52 ± 0.15	-2.43
275	15400 ± 200	4.16 ± 0.03	-2.44 ± 0.15	-2.27
288	15200 ± 200	4.14 ± 0.04	-2.19 ± 0.11	-2.16
292	15100 ± 100	4.23 ± 0.03	-2.92 ± 0.07	-2.80
300	15400 ± 200	4.14 ± 0.04	-2.21 ± 0.10	-2.19
304	16900 ± 200	4.29 ± 0.04	-2.57 ± 0.12	-2.46
347	16400 ± 200	4.38 ± 0.04	-2.11 ± 0.09	-2.06

a resolution of 2.5 \AA , which is close to the resolution of the data of Moni Bidin et al. (2007, 2009, 2011) and Salgado et al. (2013), which do not show such a gap in their results although they used the same analysis methods as we do. Unfortunately the gap remains in the results of the line profile fitting. Also using model atmospheres with or without convection did not affect the gap.

The stars in Fig. 4 can be split in two groups with respect to their position relative to the evolutionary sequences: The stars with effective temperatures between 9000 K and roughly 14000 K lie between the ZAHB and the TAHB, while the stars hotter or cooler than this temperature range lie above the TAHB.

In order to see how the parameters derived for the hot HB stars in NGC 288 compare to those obtained for other clusters and to the theoretical predictions we calculated the difference between the derived surface gravity and the one on the ZAHB for the given temperature. Fig. 5 compares our results to those obtained for M 80, NGC 5986 (Moni Bidin et al. 2009), NGC 6752 (Moni Bidin et al. 2007), M 22 (Salgado et al. 2013), and ω Cen (Moehler et al. 2011; Moni Bidin et al. 2011). Here the NGC 288 results look like those from ω Cen for temperatures below 9000 K or above about 14000 K , while

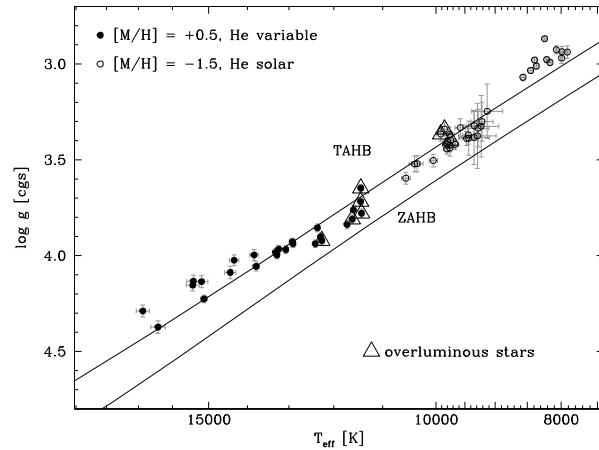


Fig. 4. Atmospheric parameters derived from the line profile fitting for the stars hotter (full symbols) and cooler (open symbols) than the u -jump. For comparison we also show a canonical zero-age horizontal branch and terminal age horizontal branch from Moehler et al. (2003).

they coincide with the other clusters for temperatures between 9000 K and 14000 K .

Using the spectroscopically determined atmospheric parameters, y magnitudes and the distance modulus of the globular cluster ($(m - M)_V = 14.95$, Carretta et al. 2000), we derived the masses shown in Fig. 6 using the equation

$$\log \frac{M}{M_{\odot}} = \frac{3.6 \cdot 10^{-7}}{\pi \cdot g_{\odot} \cdot R_{\odot} [\text{pc}]} \cdot 10^{-0.4 \cdot (y - (m - M)_V - y_{\text{th}})}$$

where y_{th} is the theoretical y magnitude at the stellar surface from Kurucz (1993) and R_{\odot} is the solar radius in parsec. Obviously the masses are systematically too low, except for the stars just hotter than the u -jump. When comparing to results from other clusters we see that the masses of the stars in NGC 288 show a similar behaviour as the surface gravities with respect to HB stars in other globular clusters.

6. Abundances

We used the parameters derived in Sect. 5.2 for the following abundance analysis.

6.1. Helium

Helium abundances were already derived during the determination of effective temperatures and surface gravities. In addition, we determined them (together with abundances for other elements) via spectrum synthesis using the abundance fitting routine of LINFOR (see Sect. 6.2 for details). The resulting abundances are listed in Tables 3 and 4. For the cool stars the abundances should be treated with caution as the helium lines are rather weak. However, the average fitted helium abundance $\log \frac{n_{\text{He}}}{n_{\text{H}}}$ of -1.03 agrees well with our assumption of solar helium abundance for the cool stars. For the hot stars the helium abundance derived with LINFOR are in general slightly higher than the ones derived with fitsb2, but in 80% of the cases the

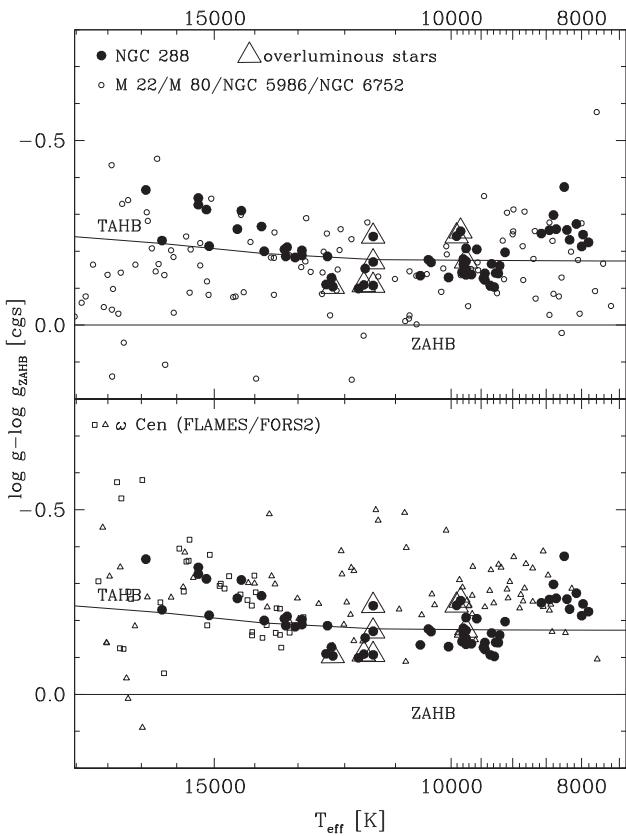


Fig. 5. Surface gravity relative to the zero-age horizontal branch at the given effective temperature. For comparison we also show a canonical zero-age and terminal-age horizontal branch from Moehler et al. (2003). In the upper plot we show also results from FORS2 observations of hot HB stars in M 80, NGC 5986 (Moni Bidin et al. 2009), NGC 6752 (Moni Bidin et al. 2007), and M 22 (Salgado et al. 2013). In the lower plot we also provide the results obtained from FLAMES and FORS2 observations of hot horizontal branch stars in ω Cen (Moehler et al. 2011, small squares; Moni Bidin et al. 2011, small triangles).

difference is below the error provided by fitsb2. On average the LINFOR abundances are higher by 0.06 dex, i.e. well below the error of the fitsb2 results.

As helium abundances have been derived for HB stars in many globular clusters with similar methods and model spectra as used in this paper, we compare our results to published data in Fig. 7. The helium abundances of Moni Bidin et al. (2007, 2009, 2012) and Moehler et al. (2000, 2003) were derived from low resolution data with 2.6 \AA – 3.4 \AA resolution. The abundances of Behr (2003) were derived from data with a resolution of 0.1 \AA , while the data used in this paper have a resolution of about 0.7 \AA . Between $11\,000\text{ K}$ and $13\,500\text{ K}$ the abundances show a clear correlation with the resolution of the data from which they were derived – the abundances decrease with increasing resolving power. **This behaviour had been noticed already by Moni Bidin et al. (2012).** This may be caused by the fact that at these relatively cool temperatures the helium lines are rather weak, which together with the helium deficiency makes them hard to fit. For higher temperatures the abundances from the different sources overlap, with the exception of the hottest star of Behr (2003). Due to the small number of results from high-resolution spectroscopy it is not clear if the resolution effect persists to higher temperatures. For a comparison to the predictions by diffusion theory see Sect. 6.4.

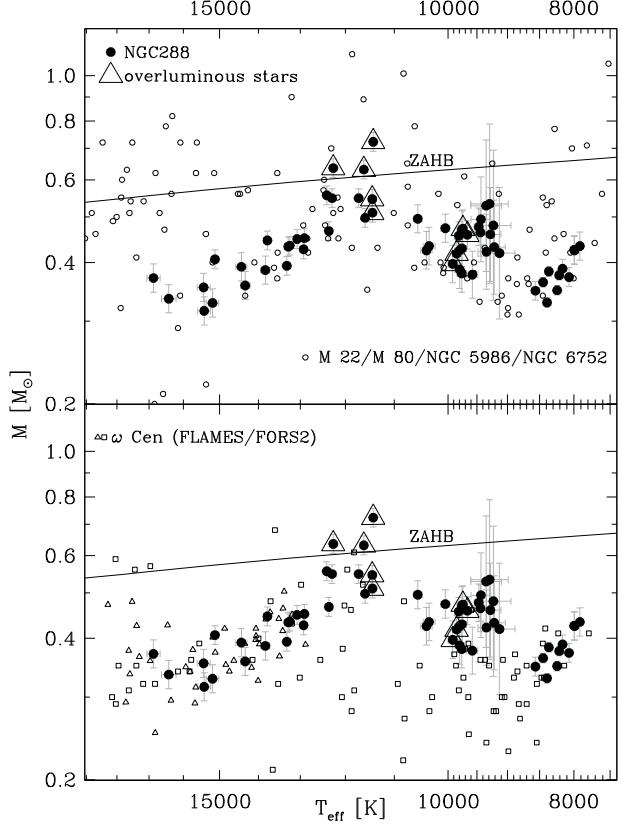


Fig. 6. Masses from line profile fits. For comparison we also show a canonical zero-age horizontal branch from Moehler et al. (2003). In the upper plot we show also results from FORS2 observations of hot HB stars in M 80, NGC 5986 (Moni Bidin et al. 2009), NGC 6752 (Moni Bidin et al. 2007), and M 22 (Salgado et al. 2013). In the lower plot we also provide the results obtained from FLAMES and FORS2 observations of hot horizontal branch stars in ω Cen (Moehler et al. 2011, small squares; Moni Bidin et al. 2011, small triangles).

Although the spectra have only medium resolution we estimated abundances via spectrum synthesis using the abundance fitting routine of LINFOR in order to verify whether our assumptions about the overall increase in heavy elements was roughly correct. We used the line lists from Kurucz (1993) and determined simultaneously abundances for He I, Mg II, Si II, P II, Ti II, Mn II, Fe II, and Ni II. Once the fitted abundances did not change anymore from one iteration to the next, we performed a visual check to verify that the spectrum had indeed been well reproduced. The results are shown in Fig. 8. The LINFOR abundance fitting routine provides only an overall error, but the scatter of abundances below $11\,000\text{ K}$ gives an idea of the minimum uncertainties, as we do not expect the abundances in shown in Fig. 8 to vary in the cool stars. For the stars hotter than

6.2. Heavy elements

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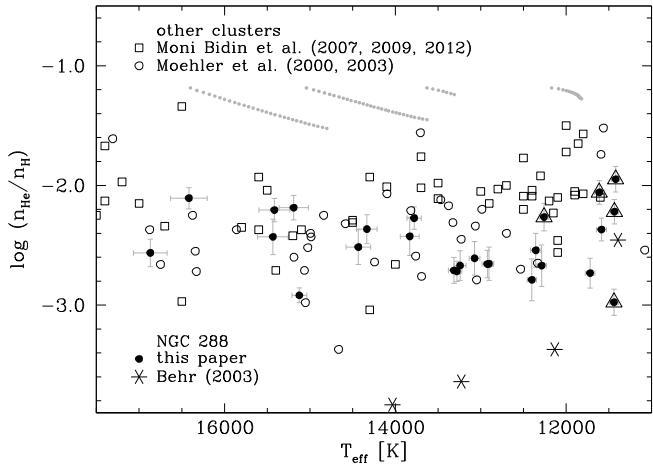


Fig. 7. Helium abundances for hot HB stars in M 80, NGC 5986, NGC 6752, and ω Cen (Moni Bidin et al.), M 3, M 13, and NGC 6752 (Moehler et al.) and NGC 288. The grey dots mark the abundances predicted for various HB ages from diffusion theory (with an ad hoc surface mixing zone, Michaud et al. 2011, see Sect. 6 for details). The tracks have dots every 3 Myr.

the u -jump additional uncertainties come from the fact that we use homogeneous model atmospheres to analyse stars affected by diffusion.

The results for P II, Ti II, Mn II, Fe II, and Ni II agree roughly with our assumption of $[M/H] = +0.5$ for the stars hotter than the u -jump, while Mg II and Si II, on the other hand, are rather lower than our assumed abundances. However, since the atmospheric structure depends more on iron than on the light elements we take these results as indication that our assumptions were reasonable. For the cool stars, Mg II and Ti II seem to show an unexpected gradient with temperature, but it is unclear if this is significant.

Our results show some differences compared to those obtained for NGC 288 by Behr (2003). Behr (2003) found no clear dependence of the Mg abundance relative to T_{eff} for the three clusters studied with a sufficient number of stars with T_{eff} above the u -jump, while a trend appears to be present in our results for NGC 288. For Si and Mn Behr found significantly lower abundances than we do, which might be an effect of instrumental resolution (see Sect. 6.1).

6.3. Abundances predicted by stratified model spectra

In order to compare the results from our observed spectra to the predictions from stratification theory we also determined abundances from model spectra of LeBlanc et al. (2009) that include abundance stratification due to diffusion. These models calculate self-consistently the structure of the atmosphere with the vertical abundance stratification. The abundances of the individual elements are calculated in each layer of the atmosphere while assuming equilibrium (a nil diffusion velocity). This leads to vertical abundance stratification and modifies the atmospheric structure. First we compared the observed metal lines to those predicted by diffusion models and found

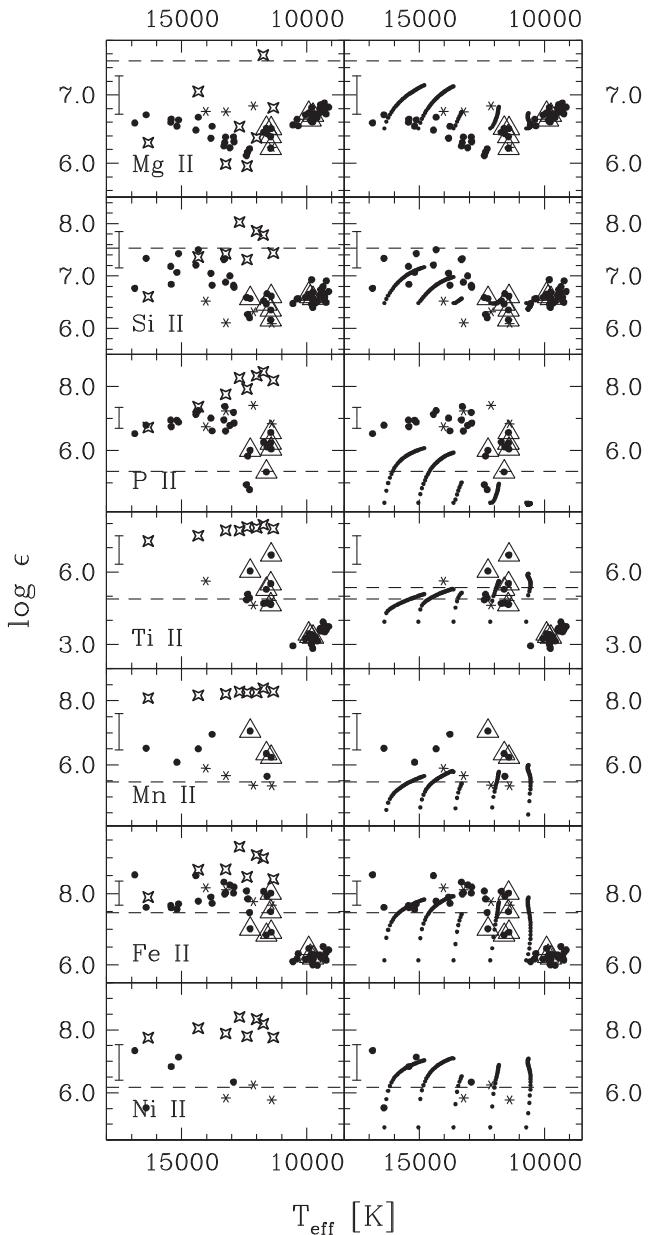


Fig. 8. Abundances derived via spectrum synthesis for all stars hotter than 9 000 K. The triangles mark the same stars as in Fig. 1. The asterisks mark the results from Behr (2003). The bars at 17 500 K mark the average error bars of Behr (2003) for NGC 288. Our errors are unlikely to be smaller. The dashed lines mark the solar abundances. The 4-pointed stars mark the abundances derived for stratified model spectra (left column, see Sect. 6 for details), which give an indication of the equilibrium abundances achievable by diffusion. The grey dots (right column) mark the abundances predicted for various HB ages from diffusion theory (with an ad hoc surface mixing zone, Michaud et al. 2011, see Sect. 6.4 for details). The tracks have dots every 1 Myr.

that the observed lines were much weaker than predicted by these models (see Fig. 9).

As discussed in LeBlanc et al. (2009), the abundances of some elements (Fe for example) predicted by the models can be overestimated because in a real star the diffusion process is a

Table 5. Temperatures and surface gravities obtained from fitting stratified model spectra with homogeneous model spectra for $[M/H] = +1$ (see Sect. 6 for details). The errors are derived from the χ^2 fit (see Sect. 5.2 for details) and are statistical errors only.

Model	Fit	
	T_{eff}	$\log g$
A	12000	3.5
B	12000	4.0
C	12000	4.5
D	13000	3.5
E	13000	4.0
F	13000	4.5
G	14000	4.0
H	14000	4.5
I	16000	4.5
J	18000	5.0

time-dependent phenomenon. Even though the radiative forces on a given element can theoretically support a very large overabundance, this situation may be hampered by various factors. The equilibrium solution used in these models may therefore not be reached. For instance, in a real star, such a large quantity of atoms might not be able to come to the surface due to the diffusion that takes place below the stellar atmosphere. Also, the abundances of other elements (such as helium) which have relatively weak radiative accelerations can be underestimated by these models.

Next we convolved the stratified model spectra to the same resolution as our observed data and multiplied them with a spectrum of average 1 and rms of 0.0125, resulting in a signal-to-noise ratio of 80. Then we determined their effective temperatures and surface gravities in the same way as described in Sect. 5.2, except that we used a model grid with $[M/H] = +1$, since the lines in the stratified model spectra were much stronger than in the observed spectra (see Fig. 9). The resulting parameters are given in Table 5 and clearly show that the analysis of stratified model spectra with homogeneous model spectra yields lower temperatures and surface gravities, with the difference in temperature increasing with increasing temperature.

Using the parameters in the right column of Table 5 we then determined abundances for those model spectra with fitted $\log g$ above 3.45 as expected for stars on or near the ZAHB at the fitted temperatures, i.e. all models except A and D. We alternated between simultaneously fitting the ions Mg II , Si II , P II , S II , A II , Ti II , V II , Cr II , and simultaneously fitting the ions Mn II , Fe I , Fe II , Co II , Ni II , Sr II , Zr II , until the fit could not be improved. Then we checked again visually that most of the spectrum had been reproduced. Usually we found that some lines were not fit well, but that is to be expected since the abundance distribution in the model atmospheres creating these spectra is far from homogeneous, resulting in a very different atmospheric structure. The results of these fits are marked by four-pointed stars in the left column of Fig. 8. As already suggested by the comparison shown in Fig. 9 the abundances derived from the stratified spectra are generally higher than those derived from the observed spectra, with He I (virtually absent

from stratified model atmospheres) and Mg II being the exceptions.

6.4. Abundances predicted by diffusion models

It is also possible to compare our abundance results to stellar evolution models computed including the effects of atomic diffusion (Michaud et al 2008, 2011). These models followed the evolution from the zero-age main sequence treating in detail atomic diffusion inside the star. On the horizontal branch, they predicted large overabundances of metals, often larger than observed above 11 000 K (similar to the problems found above for the stratified model atmospheres). A surface mixed mass of around $10^{-7} M_{\odot}$ was needed to reduce the expected anomalies to values observed in HB stars of a number of clusters as well as in sdB stars. However, the introduction of a surface mixing layer leads to a vertically homogeneous atmosphere. This is in contradiction to the observed vertical stratification of certain elements, including iron, in some blue HB stars (Khalack et al. 2007, 2008, 2010). The tracks shown in Fig. 8 are from Michaud et al. (2011). Those tracks start with the original cluster abundances at the ZAHB and cover the first third of horizontal-branch evolution which lasts some 100 Myr².

Fig. 8 shows that the abundances change more rapidly during the first 10 Myr than during the following 20 Myr for all species that become overabundant. This is largely caused by a reduction of the radiative accelerations as the concentrations increase. The abundance increase is also expected to be slow during the following 70 Myr for those species. The Si , Ti , Fe , and Ni observations are within the expected abundance range when one takes error bars evaluated from the scatter of Fe and Si below 11 000 K into account. For Si the trend suggested by the models appears to be present in the data. For Mn our abundances are higher than the results from Behr et al. (2003), which agree well with the predictions. Phosphorus is some 5 times more overabundant than predicted by the models, whereas magnesium shows small effects while the models predict larger abundances by a factor of order 5.

Helium is observed to be more underabundant than expected after 30 Myr (cf. Fig. 7). However its abundance has a very different time dependence from that of metals. The underabundance of helium is caused by gravitational settling and this process is as rapid from 10 to 30 Myr as during the first 10 Myr. Since helium settles, the settling goes as $e^{-t/\theta}$ where θ is the settling time scale. So the settling continues exponentially and if helium is underabundant by a factor of 3 after 30 Myr it should be underabundant by a factor of around 27 after 100 Myr, corresponding to a value of 9.56 in Fig. 8 at the end of the horizontal branch evolution. Since it is highly unlikely, however, that most of the stars in Fig. 8 are at the end of their HB evolution, some discrepancy remains.

As may be seen from Fig. 4 of Michaud et al (2011), abundance anomalies caused by atomic diffusion are not limited to a thin surface phenomenon. However, there are species (e.g.

² The models around 12 000 and 13 500 K were stopped around 10 Myr because of convergence problems, but the trend can be estimated from the surrounding models.

Mg) whose observed anomalies do not agree with the expected ones suggesting that the model may be missing something. Assuming that the outer $10^{-7} M_{\odot}$ is completely mixed could be an oversimplification, especially since the mixing mechanism is currently unknown. It could for instance be thermohaline convection (see Sect 5.3 of Michaud et al 2011). This is relatively weak convection which might not eliminate all effects of additional diffusion in the atmosphere. For instance, helium is largely neutral in the atmosphere of HB stars of 11 000 to 15 000 K so that it has an atomic diffusion coefficient larger than that of ionized metals (by a factor of around 100); helium might then be the most affected atomic species as turbulence weakens. This remains speculative.

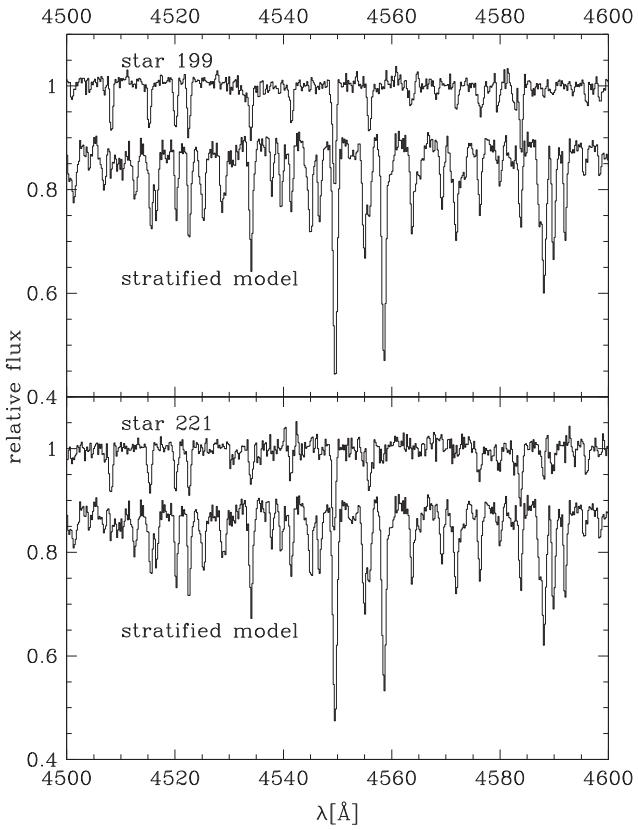


Fig. 9. Normalised spectra for stars 199 (upper panel, 12 400 K) and 221 (lower panel, 13 400 K) compared to stratified model spectra F (upper panel) and H (lower panel), which have fitted parameters close to the ones of the observed spectra. For clarity, the stratified model spectra have been offset by 0.1 from the observed spectra (see Tables 4 and 5).

7. Line profile fitting with stratified model spectra

We also verified how the use of stratified instead of homogeneous model atmospheres to fit our observations influences the parameters determined from these fits. In order to allow a direct comparison to results obtained using homogeneous model spectra without metal lines to fit our observations, we calculated a set of synthetic spectra with only H present (the abundance of all of the other elements were set at -5.00 while H is

at 12.00) while using the relations between temperature, density, and radius from the stratified model atmospheres. Helium lines were not included as the stratification abundances of helium are extremely low. For comparison we also fitted the observed spectra again (H lines only) with homogeneous model spectra computed with $[M/H] = +0.5$ and $\log \frac{n_{\text{He}}}{n_{\text{H}}} = -3$. The results are shown in Fig. 10. The prediction of larger spectroscopic gravities by the models including abundance stratification shown here was also found in Hui-Bon-Hoa et al. (2000) and LeBlanc et al. (2010). The amplitude of the effect might be overestimated by the stratified models due to the fact that, in most cases, they predict larger abundance anomalies for blue HB stars than observed (see Sect. 6).

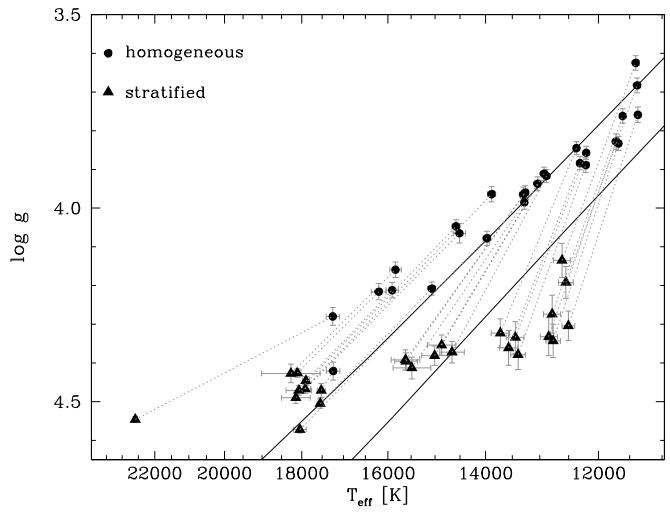


Fig. 10. Atmospheric parameters derived from the line profile fitting for the stars hotter than the u -jump, using homogeneous model atmospheres ($[M/H] = +0.5$, $\log \frac{n_{\text{He}}}{n_{\text{H}}} = -3$, filled circles) and stratified model atmospheres (filled triangles). For comparison we also show a canonical zero-age horizontal branch and terminal age horizontal branch from Moehler et al. (2003).

In Fig. 10 all stars move to higher temperatures and surface gravities when fitted with model spectra from stratified model atmospheres (as expected from the results of the reverse fitting given in Table 5), but only the stars between 14 000 K and 16 000 K move actually closer to the ZAHB. Cooler stars show too high surface gravities, while hotter ones move parallel to the TAHB. The principal defect of the stratified models is that they generally predict larger abundances than observed. In more realistic models, one would expect that the shifts shown in Fig. 10 be somewhat smaller. The lower temperature stars could then possibly fall between the TAHB and ZAHB in the $\log g - T_{\text{eff}}$ plane thus giving satisfactory results.

As a consistency check we derived masses for the new parameters, adjusting the theoretical y -magnitudes of Kurucz (1993) for $[M/H] = +0.5$ by $-0^m 3$ to account for the stratification effects. This offset was determined by comparing the fluxes of stratified and homogeneous model spectra. The results are shown in Fig. 11. Here the values obtained from stratified model spectra for stars above 14 000 K are now closer to the

canonical values than those obtained from homogeneous model spectra. This provides some support to the notion that the too low surface gravities and masses found from analyses with homogeneous model spectra are due to the mismatch in atmospheric structure between homogeneous and stratified model atmospheres. One should keep in mind, however, that the stratified model atmospheres predict in general much stronger lines than are observed, so it is currently not clear if a fully self-consistent solution can be achieved. Similarly to the discussion related to the large shifts found in Fig. 10, the masses predicted in Fig. 11 by more realistic stratified models for stars just above the temperature threshold of the u -jump, in which the abundances are less extreme, would be closer to the ZAHB.

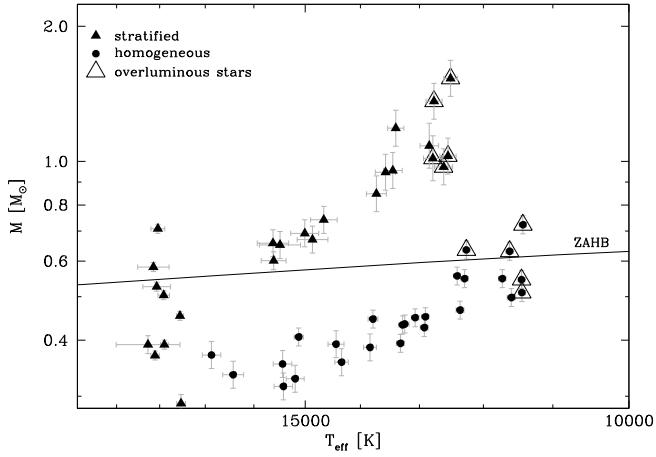


Fig. 11. The masses determined from line profile fits for the stars bluer than the Grundahl jump, using homogeneous (filled circles) and stratified (filled triangles) model spectra.

8. Overluminous Stars

One possible explanation for the overluminous stars mentioned in Sect. 1.2 is that they have evolved from hotter locations blueward of the u -jump and are now near the end of their HB phase evolving towards the asymptotic giant branch. As the evolution away from the zero-age HB increases the *overall* luminosity of an HB star, one would expect such evolved stars to be overluminous in other bandpasses besides u compared to stars near the zero-age HB. Fig. 12 shows the relation between the effective temperature derived from line profile fits and the y magnitude of the HB stars. Here especially the hot overluminous stars are clearly brighter than the 'normal' stars at similar temperatures. To a lesser extent this is also true for the cool overluminous stars. In Figs. 4 and 5, however, only three of the overluminous stars, namely 100 (hot), 103, and 127 (both cool) are clearly separated from the majority of the stars by a significantly lower surface gravity. It is not obvious why the other overluminous stars have higher luminosities, as they are inconspicuous with respect to the majority of the stars in all other parameters (effective temperature, surface gravity, and abundances). However, even three stars evolving off the ZAHB in

the temperature range 9 700 K to 11 500 K pose a problem for evolutionary time scales, as one would expect to find of the order of 100 HB stars close to the ZAHB between about 11 000 K and 14 000 K (corresponding to a range of roughly 0.5 – 1.05 in $u - y$ in Fig. 1) for each of the evolved stars, which are clearly not seen.

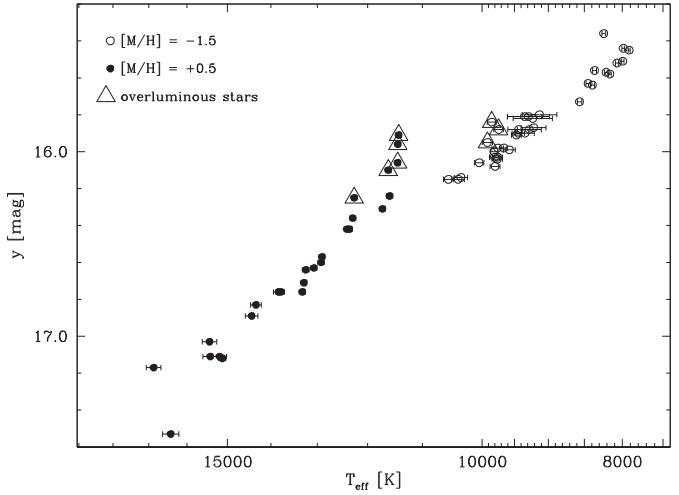


Fig. 12. The y magnitudes of the HB stars compared to the effective temperatures derived from line profile fits.

If the overluminous stars are post-HB stars evolved from a hotter location along the blue tail (as suggested by their higher luminosity), one would expect them to preserve their abundance anomalies as they approach the u -jump until dredge-up from the deepening hydrogen convection zone causes the surface abundances to return approximately to the normal cluster abundances. However such stars are expected to have had a low He abundance on the HB and a low rotation rate which may cause them to maintain their abundance anomalies to temperatures somewhat lower than the u -jump. First, due to the depletion of their surface helium, the overluminous stars just redward of the u -jump may have slightly shallower convection zones than the other stars of the same effective temperature. However hydrogen ionization is the main driver of the convection when the effective temperature is below 10 000 K and it will lead to progressive helium dredge-up so that the difference in convection zone depth could be small below 10 000 K. Second, due to the rotation rate drop in HB stars blueward of the u -jump, the overluminous stars would be expected to have low rotation rates, if they are evolved from the blue HB. This, in turn, would reduce the meridional flows which inhibit diffusion in stars cooler than the u -jump. However, as may be seen from Fig. 4 of Quievy et al. (2009), the limiting rotation rate decreases very rapidly as the effective temperature drops below 10 000 K; a star with a $v_e = 8 \text{ km s}^{-1}$ would show large effects of diffusion above 12 000 K but would be mixed below 10 000 K. The results given in Fig. 8 indeed show that the effects of radiative diffusion disappear between the overluminous stars hotter than the u -jump at 11 500 K and the overluminous stars cooler than the u -jump at 10 000 K. So it would appear that the low

He abundance due to diffusion and low rotation do not prevent the effects of diffusion from disappearing rather quickly as a star evolves through the u -jump to cooler temperatures. This result supports the general assumption that the abundances of HB stars redward of the u -jump are not affected by diffusion, irrespective of their evolutionary status. **The observations are ahead of the stellar evolution models in this case. To put the theory on a stronger base, one would need to continue the evolution calculations with diffusion to the end of the HB; however one would also need to include meridional circulation to verify at what effective temperature the mixing occurs and how this temperature depends on rotation.**

9. Summary and Conclusions

- The atmospheric parameters and masses of the hot HB stars in NGC 288 show a behaviour seen also in other clusters for temperatures between 9 000 K and 14 000 K. Outside this temperature range, however, they follow the results found for such stars in ω Cen.
- The abundances derived from our observations are for most elements within the abundance range expected from evolutionary models that include the effects of atomic diffusion and assume a surface mixed mass of $10^{-7} M_\odot$ as determined previously for sdB stars and other clusters. The exceptions are helium, which is more deficient than expected and phosphorus, which is substantially more abundant than predicted. The abundances predicted by stratified model atmospheres, which were not adjusted to observations, are generally significantly more extreme than observed, except for magnesium.
- Analysing the observed spectra with stratified model spectra moves the HB stars to higher temperatures, surface gravities, and masses. Since the equilibrium abundances lead to excessive adjustments, more realistic abundance gradients may well lead to models that put the HB stars between the TAHB and ZAHB (see Sect. 7). Model atmospheres including such improvements are needed to answer this question.
- Five of the eight overluminous stars around the u -jump, which we observed, do not deviate substantially from the other HB stars in the same temperature range in any of the parameters we determined. We are therefore at a loss to explain their brighter luminosities. The remaining three overluminous stars do show lower surface gravities, as would be expected if they evolve away from the HB. However, they pose a substantial problem for evolutionary time scales, as one would expect to find of the order of 100 HB stars close to the ZAHB between about 11 000 K and 14 000 K (corresponding to a range of roughly 0.5 – 1.05 in $u - y$ in Fig. 1) for each of the evolved stars, which are clearly not seen.
- With respect to their abundances all overluminous stars show the same behaviour as the majority of the stars in the respective temperature range. **This result supports the general assumption that the abundances of HB stars redward of the u -jump are not affected by diffusion, irrespective of their evolutionary status.**

The evolution models including diffusion and the stratified model atmospheres both predict higher than observed abundances for many elements affected by radiative levitation. The evolution models can be adjusted to reproduce the observed abundances by introducing an ad hoc defined mixed zone, which, however, is potentially inconsistent with the observed vertical stratification of at least some elements in the atmosphere. For the stratified model atmospheres, it is currently unclear whether a more limited abundance stratification which would provide a better description of the observed abundances could still explain the photometric anomalies around the u -jump. Our results show definite promise towards solving the long-standing issue of surface gravity and mass discrepancies for hot HB stars, but there is still much work needed to arrive at a self-consistent solution.

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Table 1. Target coordinates and photometric data.

ID	α_{2000}	δ_{2000}	y	$b - y$	c_1	m_1
52	00:52:50.77	-26:38:02.9	15.357±0.001	+0.030±0.003	+1.301±0.005	+0.131±0.005
55	00:52:47.43	-26:33:14.2	15.318±0.002	+0.094±0.002	+1.253±0.004	+0.122±0.004
60	00:52:38.59	-26:37:05.1	15.328±0.003	+0.110±0.004	+1.202±0.008	+0.118±0.007
61	00:52:42.80	-26:36:39.2	15.312±0.001	+0.127±0.002	+1.151±0.004	+0.121±0.003
63	00:52:47.08	-26:35:25.0	15.345±0.002	+0.094±0.003	+1.264±0.005	+0.119±0.005
70	00:52:45.40	-26:35:21.5	15.438±0.002	+0.055±0.003	+1.288±0.004	+0.133±0.004
72	00:52:53.92	-26:38:45.6	15.421±0.002	+0.088±0.004	+1.234±0.008	+0.125±0.008
74	00:52:35.47	-26:34:24.8	15.453±0.001	+0.055±0.002	+1.283±0.005	+0.133±0.003
79	00:52:42.68	-26:34:50.2	15.507±0.002	+0.050±0.003	+1.307±0.004	+0.135±0.005
81	00:52:40.77	-26:33:47.7	15.569±0.001	+0.034±0.002	+1.288±0.003	+0.137±0.003
83	00:52:32.07	-26:35:46.6	15.560±0.002	+0.022±0.002	+1.266±0.007	+0.139±0.004
86	00:52:52.51	-26:34:29.7	15.582±0.001	+0.038±0.002	+1.284±0.006	+0.136±0.004
88	00:52:52.10	-26:34:12.1	15.639±0.002	+0.021±0.003	+1.260±0.007	+0.131±0.005
89	00:52:37.88	-26:36:35.4	15.518±0.002	+0.042±0.002	+1.242±0.006	+0.134±0.003
90	00:52:46.64	-26:39:03.1	15.634±0.002	+0.020±0.004	+1.253±0.011	+0.131±0.009
96	00:52:37.64	-26:31:13.5	15.735±0.004	+0.005±0.004	+1.238±0.010	+0.134±0.007
99	00:52:29.92	-26:36:07.4	15.799±0.002	-0.004±0.003	+1.182±0.009	+0.133±0.007
100	00:52:38.68	-26:35:58.6	15.959±0.002	-0.034±0.002	+0.858±0.004	+0.112±0.004
101	00:53:04.16	-26:38:29.8	15.911±0.005	-0.024±0.009	+0.938±0.011	+0.116±0.015
102	00:52:51.47	-26:36:26.0	15.815±0.001	+0.007±0.002	+1.205±0.004	+0.128±0.003
103	00:52:35.45	-26:39:11.0	15.840±0.003	-0.011±0.004	+1.063±0.010	+0.115±0.007
106	00:53:02.55	-26:35:32.9	15.822±0.002	+0.005±0.003	+1.176±0.008	+0.127±0.005
107	00:52:32.39	-26:36:30.2	15.810±0.002	+0.008±0.002	+1.173±0.009	+0.126±0.004
111	00:53:05.31	-26:32:45.2	15.982±0.003	-0.017±0.004	+1.084±0.005	+0.136±0.005
113	00:52:39.48	-26:36:45.7	15.866±0.001	+0.001±0.002	+1.161±0.006	+0.125±0.004
114	00:52:38.68	-26:37:49.6	15.905±0.004	-0.002±0.006	+1.132±0.015	+0.126±0.011
115	00:52:45.24	-26:37:55.1	15.881±0.001	+0.000±0.002	+1.170±0.006	+0.125±0.005
118	00:52:55.50	-26:35:08.2	15.902±0.001	-0.005±0.002	+1.158±0.008	+0.124±0.003
119	00:52:56.84	-26:33:44.8	15.883±0.001	+0.002±0.002	+1.159±0.007	+0.123±0.004
120	00:53:01.85	-26:37:53.2	15.913±0.004	-0.008±0.006	+1.136±0.007	+0.128±0.010
122	00:52:37.78	-26:39:31.6	15.880±0.002	-0.012±0.004	+1.094±0.011	+0.127±0.009
127	00:52:39.32	-26:34:31.6	15.953±0.002	-0.014±0.002	+1.047±0.004	+0.111±0.004
142	00:52:50.55	-26:36:49.8	16.061±0.002	-0.032±0.002	+0.876±0.005	+0.111±0.004
143	00:52:52.77	-26:34:53.0	16.003±0.002	-0.005±0.003	+1.084±0.006	+0.119±0.006
145	00:52:40.58	-26:32:48.6	15.981±0.002	-0.013±0.002	+1.108±0.004	+0.124±0.003
146	00:52:43.35	-26:37:56.4	16.098±0.002	-0.019±0.004	+0.878±0.005	+0.107±0.006
147	00:52:37.26	-26:36:46.9	16.033±0.002	-0.013±0.003	+1.054±0.007	+0.127±0.004
149	00:52:33.14	-26:33:44.6	16.084±0.003	-0.020±0.004	+1.044±0.009	+0.122±0.005
151	00:52:48.32	-26:32:57.6	16.032±0.002	-0.016±0.003	+1.074±0.004	+0.131±0.004
154	00:52:54.89	-26:37:11.7	16.058±0.001	-0.007±0.002	+1.054±0.007	+0.112±0.004
156	00:52:50.53	-26:35:12.0	16.039±0.003	-0.004±0.005	+1.060±0.007	+0.112±0.009
157	00:52:53.76	-26:39:08.7	15.992±0.004	-0.013±0.007	+1.073±0.011	+0.123±0.013
167	00:52:46.42	-26:34:07.7	16.093±0.002	-0.009±0.003	+1.039±0.006	+0.112±0.006
169	00:52:46.50	-26:31:30.7	16.153±0.002	-0.023±0.003	+0.957±0.006	+0.119±0.005
176	00:52:48.70	-26:34:00.7	16.140±0.002	-0.012±0.003	+0.984±0.006	+0.113±0.006
179	00:52:48.17	-26:35:19.9	16.236±0.003	-0.032±0.006	+0.844±0.009	+0.108±0.011
180	00:52:50.91	-26:36:09.4	16.153±0.002	-0.014±0.003	+0.975±0.004	+0.111±0.004
183	00:52:39.91	-26:37:23.8	16.254±0.002	-0.025±0.004	+0.784±0.011	+0.105±0.009
187	00:52:44.71	-26:35:31.4	16.307±0.003	-0.033±0.005	+0.843±0.008	+0.116±0.009
195	00:52:27.41	-26:35:58.8	16.422±0.004	-0.050±0.005	+0.685±0.008	+0.122±0.008
196	00:52:44.29	-26:35:53.2	16.357±0.002	-0.031±0.002	+0.760±0.004	+0.105±0.004
199	00:52:55.57	-26:32:58.7	16.425±0.002	-0.042±0.002	+0.726±0.005	+0.113±0.004
212	00:52:59.33	-26:39:00.4	16.605±0.005	-0.068±0.009	+0.577±0.013	+0.135±0.017
213	00:52:42.83	-26:31:06.8	16.627±0.005	-0.062±0.005	+0.564±0.008	+0.128±0.007

Table 1. Target coordinates and photometric data (cont'd)

ID	α_{2000}	δ_{2000}	y	$b - y$	c_1	m_1
216	00:52:54.57	-26:33:20.4	16.572 \pm 0.002	-0.051 \pm 0.005	+0.627 \pm 0.011	+0.117 \pm 0.010
221	00:52:52.31	-26:35:13.7	16.638 \pm 0.002	-0.037 \pm 0.003	+0.584 \pm 0.007	+0.105 \pm 0.006
228	00:52:47.36	-26:37:52.6	16.761 \pm 0.002	-0.057 \pm 0.004	+0.495 \pm 0.009	+0.116 \pm 0.008
230	00:52:24.33	-26:35:23.5	16.759 \pm 0.009	-0.059 \pm 0.014	+0.485 \pm 0.029	+0.114 \pm 0.025
231	00:52:47.01	-26:36:23.0	16.714 \pm 0.003	-0.057 \pm 0.004	+0.552 \pm 0.008	+0.115 \pm 0.006
240	00:52:43.69	-26:35:01.7	16.761 \pm 0.003	-0.053 \pm 0.005	+0.534 \pm 0.007	+0.113 \pm 0.008
242	00:52:45.02	-26:37:35.4	16.828 \pm 0.002	-0.064 \pm 0.005	+0.421 \pm 0.007	+0.121 \pm 0.009
243	00:52:44.02	-26:35:42.2	16.889 \pm 0.003	-0.043 \pm 0.003	+0.445 \pm 0.006	+0.105 \pm 0.005
275	00:52:49.39	-26:35:53.7	17.030 \pm 0.006	-0.045 \pm 0.009	+0.391 \pm 0.015	+0.098 \pm 0.016
288	00:52:49.30	-26:38:19.1	17.115 \pm 0.003	-0.058 \pm 0.004	+0.358 \pm 0.006	+0.104 \pm 0.006
292	00:53:00.03	-26:36:32.9	17.117 \pm 0.003	-0.068 \pm 0.005	+0.406 \pm 0.008	+0.108 \pm 0.008
300	00:52:49.11	-26:35:35.1	17.106 \pm 0.003	-0.048 \pm 0.007	+0.362 \pm 0.009	+0.100 \pm 0.013
304	00:52:48.60	-26:33:17.1	17.173 \pm 0.003	-0.054 \pm 0.005	+0.307 \pm 0.011	+0.107 \pm 0.009
347	00:52:50.31	-26:38:30.0	17.532 \pm 0.003	-0.066 \pm 0.005	+0.275 \pm 0.009	+0.102 \pm 0.009

Table 2. Observing times, conditions and setups

Date	Start [UT]	Seeing	Airmass	Moon		setup	exposure time [s]
				Illum.	Dist.		
2003-07-04	08:15:23	1''.5	1.15	0.21	146°9	LR1	2520
2003-07-04	09:06:06	1''.1	1.06	0.22	147°3	LR1	2520
2003-07-04	09:49:14	1''.1	1.02	0.22	147°7	LR1	2000
2003-07-05*	07:11:48	1''.0	1.37	0.30	153°2	LR1	2520
2003-07-05*	07:56:47	1''.2	1.21	0.30	153°4	LR1	1432
2003-07-07	08:04:26	0''.9	1.15	0.52	149°7	LR1	2520
2003-07-07	08:49:35	0''.8	1.06	0.53	149°4	LR1	2520
2003-07-07	09:33:38	0''.8	1.02	0.53	149°2	LR1	2520
2003-07-07*	10:16:53	0''.8	1.00	0.53	148°9	LR1	832
2003-07-08	08:23:19	0''.6	1.10	0.63	140°2	LR1	2520
2003-07-08	09:09:37	0''.7	1.03	0.64	139°8	LR1	2520
2003-07-08*	09:53:34	0''.8	1.01	0.64	139°4	LR1	1417
2003-07-09	09:19:31	0''.7	1.02	0.75	128°2	LR1	2520
2003-07-10	09:06:35	0''.6	1.03	0.84	115°9	LR3	3000
2003-07-10	10:01:51	1''.1	1.00	0.84	115°3	LR3	661
2003-07-20	05:36:53	0''.7	1.59	0.59	30°1	LR3	2520
2003-07-20	06:20:22	1''.0	1.40	0.59	30°3	LR3	623
2003-07-21*	06:15:02	0''.6	1.34	0.50	38°0	LR3	2520
2003-07-21	06:58:04	0''.8	1.18	0.49	38°2	LR3	2520
2003-07-21	07:47:32	1''.2	1.07	0.49	38°5	LR2	2520
2003-07-21	08:30:33	1''.5	1.02	0.49	38°7	LR2	2520
2003-07-21	10:17:49	1''.1	1.02	0.48	39°3	LR2	1736
2003-07-22	05:03:19	0''.4	1.83	0.41	46°6	LR1	2520
2003-07-22	05:46:25	0''.4	1.47	0.40	46°9	LR1	2520
2003-07-22	06:37:10	0''.5	1.24	0.40	47°3	LR2	2520
2003-07-22	07:22:53	0''.5	1.11	0.40	47°6	LR2	2520
2003-07-22	08:12:00	0''.5	1.04	0.40	47°9	LR2	2520
2003-07-22*	10:21:07	0''.6	1.02	0.39	48°6	LR2	20
2003-07-27	07:45:34	0''.9	1.04	0.04	101°2	LR1	2520
2003-07-28	05:59:11	0''.5	1.29	0.01	111°3	LR2	2520
2003-07-28	06:49:13	0''.5	1.13	0.01	111°9	LR1	2520

*: not used in final analysis, usually due to S/N

Table 3. Temperatures and surface gravities for stars redder than the u -jump and not showing any evidence of radiative levitation as derived from the a_0 and sz parameters and from line profile fits for an assumed metallicity of $[M/H] = -1.5$. The errors for the photometric results are derived from the errors of a_0 and sz in combination with the errors of the fits and an uncertainty of 0^m02 for the reddening (see Sect. 5.1 for details). The errors for the spectroscopic results are derived from the χ^2 fit (see Sect. 5.2 for details) and are statistical errors only. In addition we list the helium abundance as determined with LINFOR (see Sect. 6 for details).

ID	Photometric Parameters			Spectroscopic Parameters			
	a_0 [mmag]	sz [mmag]	T_{eff} [K]	$\log g$	T_{eff} [K]	$\log g$	$\log(\frac{n_{\text{He}}}{n_{\text{H}}})_{\text{LINFOR}}$
52	+48± 4	91± 5	9100±380	3.39±0.11	8240± 20	2.87±0.02	
55	+124± 4	91± 4	8100±260	3.08±0.15			
60	+134± 6	89± 7	8000±260	3.05±0.19			
61	+151± 3	79± 3	7900±210	3.09±0.16			
63	+125± 5	95± 5	8100±270	3.02±0.17			
70	+82± 4	86± 4	8600±330	3.36±0.12	7990± 20	2.94±0.03	
72	+114± 7	86± 8	8200±300	3.21±0.18			
74	+81± 3	85± 3	8600±320	3.37±0.11	7910± 10	2.94±0.04	
79	+79± 5	86± 5	8600±340	3.37±0.13	7990± 10	2.97±0.03	
81	+54± 3	84± 3	9000±350	3.47±0.10	8210± 20	2.98±0.02	
83	+34± 4	80± 4	9300±400	3.57±0.10	8360± 30	3.02±0.02	
86	+57± 3	84± 4	8900±360	3.46±0.10	8160± 20	3.00±0.02	
88	+30± 5	88± 6	9300±420	3.46±0.11	8390± 30	2.98±0.02	
89	+56± 3	81± 3	8900±360	3.51±0.10	8070± 20	2.93±0.03	
90	+27± 7	87±10	9400±470	3.48±0.14	8450± 30	3.04±0.02	
96	+5± 7	84± 7	9700±500	3.54±0.12	8560± 30	3.07±0.02	
99	-17± 6	80± 7	10100±510	3.61±0.12	9130±260	3.25±0.15	-0.6
102	0± 3	86± 3	9800±440	3.51±0.09	9290±320	3.38±0.18	-1.4
103	-56± 6	86± 7	10900±590	3.42±0.19	9850± 70	3.34±0.04	-1.0
106	-8± 5	84± 6	10000±490	3.54±0.11	9230±290	3.33±0.17	-1.3
107	-5± 4	85± 4	9900±460	3.52±0.10	9350±260	3.39±0.15	-1.2
111	-52± 6	68± 6	10800±570	3.82±0.12	9760± 90	3.44±0.05	-1.0
113	-17± 3	85± 4	10100±470	3.52±0.11	9210±180	3.31±0.11	-0.8
114	-27± 9	81±11	10300±600	3.58±0.17	9340±140	3.33±0.08	-1.0
115	-16± 4	86± 5	10100±480	3.50±0.12	9280±180	3.34±0.10	-1.1
118	-27± 3	86± 3	10300±480	3.49±0.11	9440± 90	3.38±0.05	-1.1
119	-16± 3	87± 4	10100±470	3.48±0.11	9430±170	3.39±0.09	-1.2
120	-32± 9	80±10	10400±600	3.60±0.17	9470± 70	3.39±0.04	-1.0
122	-47± 7	77± 9	10700±590	3.64±0.17	9740± 80	3.40±0.04	-1.1
127	-63± 4	89± 4	11000±550	3.33±0.18	9920± 80	3.37±0.04	-0.8
143	-42± 5	84± 6	10600±550	3.50±0.16	9810± 60	3.45±0.03	-1.1
145	-46± 3	82± 3	10700±520	3.54±0.12	9660± 60	3.42±0.03	-1.0
147	-54± 4	73± 5	10800±550	3.71±0.12	9810± 80	3.43±0.04	-0.8
149	-67± 5	78± 5	11100±590	3.58±0.17	9800± 80	3.41±0.04	-1.0
151	-53± 4	72± 4	10800±540	3.74±0.11	9760± 80	3.43±0.04	-0.9
154	-51± 3	88± 4	10800±520	3.39±0.15	10100±100	3.51±0.04	-1.1
156	-46± 8	88±10	10700±610	3.40±0.22	9760± 80	3.37±0.04	-1.0
157	-52±11	79±13	10800±670	3.59±0.23	9580± 90	3.34±0.05	-1.1
169	-88± 4	72± 5	11600±600	3.69±0.17	10400±100	3.53±0.05	-1.0
176	-72± 5	80± 6	11200±600	3.52±0.19	10300±100	3.52±0.05	-1.0
180	-75± 4	82± 5	11300±580	3.46±0.18	10600± 80	3.60±0.04	-1.1